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# Role of Hydrophobic Interactions in Enzyme Inhibition by Drugs 

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#### Abstract

The role of hydrophobic interactions in inhibiting the relatively specific enzymatic reactions of five enzyme systems by series of congeneric drugs has been illustrated by the use of substituent constants and regression analysis. The inhibition of lipoxygenase by alcohols, the inhibition of D -amino acid oxidase by maleimides, and the inhibition of hydroxyindole- $o$-methyltransferase by $N$-acyltryptamines are found to be linearly dependent on the lipohydrophilic character of the inhibitors $(\log P$ or $\pi)$. The inhibition of carbonic anhydrase by sulfonamides is found to be linearly dependent on the $\log P$ and Hammett's $\sigma$ constant. For monoamine oxidase inhibition by substituted $\beta$-carbolines, a parabolic equation of $\log P$ gives the most significant correlation. The ideal lipohydrophilic character $\left(\log P_{0}\right)$ for maximum inhibition is found to be 2.74 .


KeyphrasesEnzyme inhibitory activity-hydrophobic interactions, drugs
$\qquad$ Physicochemical constants, enzyme inhibitiontory activity correlation

In recent years much effort has been focused on elucidation of weak intermolecular forces in biological systems (1), especially on the importance of hydrophobic interactions (2-6). Various experimental methods have been used to estimate the hydrophobic bonding tendency of drug molecules, such as partitioning and chromatographic methods (3, 7). Organic solvents capable of forming hydrogen bonds (e.g., alcohols and esters) appear to give better correlations than hydrocarbons (8). The purpose of this paper is to correlate quantitatively enzyme inhibitory activity with the tendency of hydrophobic interactions of series of drugs, as measured by the partition coefficient of 1 -octanol-water. It is hoped that this work may shed some light on the intermolecular forces involved in enzyme inhibition and provide some clues in designing new enzyme inhibitors.

## METHOD

The biological data given in Table I are taken from the literature (4, 9-12). The Hammett's sigma constants ( $\sigma$ ) are from the compilation of Jaffé (13) unless otherwise stated. The $\log P$ values are either experimentally determined or calculated from the $\pi$ constants
$(14,15)$ of Hansch. For example, the $\log P$ of $N$-acetyltryptamine is calculated as follows:


The steric constants, $E_{s}$, are taken from Leffler and Grunwald (16). The equations listed in Table II are derived via the method of least squares using an IBM 360/65 computer. The inhibition constant $K_{l}, k^{\prime}=\left(k_{1} / K_{I}\right)$, or the concentration of an inhibitor giving $50 \%$ inhibition of the enzyme ( $I_{50}$ ) is converted to the molar basis, and $p K_{I}, \log k^{\prime}$, or $\log 1 / I_{50}$ is used as a measure of the inhibitory activity.

## RESULTS

The equations correlating enzyme inhibition with the physicochemical constants are summarized in Table II, where $n$ is the number of data points used in the analysis, $r$ is the correlation coefficient, and $s$ is the standard deviation.

In the inhibition of lipoxygenase by monohydric alcohols, the relative inhibitory activity is mainly determined by the lipohydrophilic character $(\log P)$. More than $98 \%\left(r^{2}=0.983\right)$ of the variance in the data can be accounted for by the simple linear equation (Eq. 1a). Equation $1 b$, derived by Mitsuda et al. (4), gives a slightly lower correlation coefficient, presumably due to the slightly different $\log P$ values used.

For the carbonic anhydrase inhibition by sulfonamides, by comparing Eq. $2 a$ with Eq. $2 b$ one can see that the electronic term $\sigma$ is slightly more important than the $\log P$ term. The positive coefficient associated with $\sigma$ indicates that electron-withdrawing groups will increase the inhibitory activity. By using both terms simultaneously, a much better correlation is obtained (Eq. $2 c$ ). The $\log P$ term in Eq. $2 c$ is significant at 97.5 -percentile level, as indicated by an $F$-test ( $F_{1,16}=7.2 ; F_{1,150.975}=6.2$ )

The $\pi$-constant alone gives almost perfect correlation for inhibition of D-amino acid oxidase by $N$-alkylmaleimides (Eqs. $3 b$ and $3 c$ ). By using $\pi$ and $\sigma$ terms together, high correlation is obtained for the $N$-aryl as well as $N$-alkyl derivatives. The $\sigma$ term in Eq. $3 a$ is highly significant ( $F_{1,5}=111 ; F_{1,50.995}=63.6$ ).
For the inhibition of hydroxyindole-o-methyltransferase by $N$ acyltryptamines, $\log P$ alone gives fairly good correlation (Eq. $4 a$ ). By deleting three molecules with deviation greater than $2 s$, a better

Table I—Enzymological Data and the Physicochemical Constants Used in Deriving the Equations in Table II

| Calcd. ${ }^{a}$ | $-p K_{I}-$ | Found ${ }^{\text {b }}$ |  | $\underset{\log P^{c}}{\mathrm{R}-\mathrm{OH}}$ | R- |
| :---: | :---: | :---: | :---: | :---: | :---: |
| -0.30 |  | $-0.18$ |  | -0.66 | $\mathrm{CH}_{3}-$ |
| 0.18 |  | 0.18 |  | -0.16 | $\mathrm{C}_{2} \mathrm{H}_{5}$ |
| $0.46$ |  | 0.37 |  | 0.14 | iso- $\mathrm{C}_{3} \mathrm{H}_{7}$ |
| 0.65 |  | 0.68 |  | 0.34 | $n-\mathrm{C}_{3} \mathrm{H}_{7}$ |
| 0.72 |  | 0.49 |  | 0.41 | tert-C4 ${ }_{4}$ |
| $0.91$ |  | 0.86 |  | 0.61 | $s$ - $\mathrm{C}_{4} \mathrm{H}_{9}-$ |
| 0.94 |  | 1.13 |  | 0.64 | iso- $\mathrm{C}_{4} \mathrm{H}_{9}-$ |
| 1.13 |  | 1.15 |  | 0.84 | $n-\mathrm{C}_{4} \mathrm{H}_{9}-$ |
| $\begin{aligned} & 1.15 \\ & 1.39 \end{aligned}$ |  | 1.34 |  | 1.11 | iso- $\mathrm{C}_{5} \mathrm{H}_{11}$ - |
| 1.61 |  | 1.61 |  | 1.34 |  |
| 2.08 |  | $2.10$ |  | 1.84 | $n-\mathrm{C}_{6} \mathrm{H}_{13}$ |
| 2.56 |  |  |  | 2.34 | $n-\mathrm{C}_{7} \mathrm{H}_{15}-$ |
|  |  |  | $\mathrm{R}-\mathrm{C}$ |  |  |
| ${ }^{p} K_{I}\left(\log 1 / K_{I}\right)$ |  |  |  |  |  |
| Calcd. ${ }^{\text {a }}$ | Found ${ }^{\text {e }}$ |  | $\log P^{f}$ | $\sigma^{g}$ | R- |
| 4.72 | 4.96 |  | $-0.28$ | -0.59 | $p-\mathrm{CH}_{3} \mathrm{NH}-$ |
| 4.53 | 4.60 |  | $-0.78$ | -0.66 | $p-\mathrm{NH}_{2}-$ |
| 5.15 | 5.30 |  | 0.27 | -0.27 | $p-\mathrm{CH}_{3} \mathrm{O}-$ |
| 5.38 | 5.50 |  | 0.83 | -0.17 | $p-\mathrm{CH}_{3}-$ |
| 5.47 | 5.22 |  | 0.82 | -0.07 | $m-\mathrm{CH}_{3}-$ |
| 5.39 | 5.13 |  | 0.31 | 0.00 | $\mathrm{H}-$ |
| 5.78 | 5.96 |  | 1.01 | 0.23 | $p-\mathrm{Cl}-$ |
| 5.86 | 5.96 |  | 1.33 | 0.23 | $p-\mathrm{Br}-$ |
| 5.92 | 5.92 |  | 1.07 | 0.37 | $m-\mathrm{Cl}-$ |
| 6.07 | 5.89 |  | -0.06 | 0.87 |  |
| 5.89 | 6.19 |  | $-0.01$ | 0.65 | $p-\mathrm{CN}-$ |
| 6.05 | 6.12 |  | 0.42 | 0.71 | $m-\mathrm{NO}_{2}-$ |
| 6.15 | 6.26 |  | 0.55 | 0.78 0.50 | $p-\mathrm{NO}_{2}-$ |
| 6.22 6.44 | 6.52 6.60 |  | 1.77 1.12 | 0.50 0.94 | 3, $\mathrm{Na}_{2} \mathrm{Cl}_{2-}-\mathrm{Cl}$ |
| 6.80 | 6.66 |  | 1.62 | 1.20 | $3-\mathrm{CF}_{3}-4-\mathrm{Cl}-$ |
| 5.45 | 4.92 |  | 0.99 | -0.14 | $2-\mathrm{CH}_{3}-$ |
| 5.73 | 5.62 |  | 0.90 | 0.20 | $2 \mathrm{Cl}-$ |
| 5.82 | 5.46 |  | 0.08 | 0.55 | $2-\mathrm{NO}_{2}-$ |
|  |  |  |  |  |  |



Table I-(Continued)

| $\text { Calcd. }{ }^{n}$ | Found ${ }^{\circ}$ | $\log P$ | $\mathrm{R}_{1}$ - | $\mathrm{R}_{2}-$ | $\mathrm{R}_{3}-$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4.51 | 4.70 | 5.02 | $\mathrm{H}-$ | 3,4-- $\mathrm{Cl}_{2}-\mathrm{C}_{6} \mathrm{H}_{3}$ | H- |
| 3.75 | 3.70 | 3.76 | H- | $3,4,5-\left(\mathrm{CH}_{3} \mathrm{O}\right)_{3}-$ | H- |
| 3.71 | 3.77 | 3.69 | F- | $\mathrm{C}_{6} \mathrm{H}_{5}-$ | $\mathrm{H}-$ |
| 4.20 | 4.15 | 4.50 | $\mathrm{Br}-$ | $\mathrm{C}_{6} \mathrm{H}_{5}$ | H |
| 4.59 | 4.66 | 5.15 | F- | 3,4- $\mathrm{Cl}_{2}-\mathrm{C}_{6} \mathrm{H}_{3}-$ | $\mathrm{H}-$ |
| 5.08 | 5.30 | 5.96 | $\mathrm{Br}-$ | $3,4-\mathrm{Cl}_{2}-\mathrm{C}_{6} \mathrm{H}_{3}-$ | $\mathrm{H}-$ |
| 4.11 | 3. $57{ }^{p}$ | 4.36 | H | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CH}_{2}$ - | $\mathrm{CH}_{3}-$ |
| 4.05 | 3,42 ${ }^{\text {p }}$ | 4.26 | H- | $3,4,5-\left(\mathrm{CH}_{3} \mathrm{O}\right)_{3}$ | $\mathrm{H}-$ |
| 4.54 | $3.96{ }^{p}$ | 5.08 | H | 3,5-- $\mathrm{Cl}_{2}-\mathrm{C}_{6} \mathrm{H}_{3}-$ | H- |
| Calcd. ${ }^{q}$ | Found ${ }^{r}$ | $E_{8}$ | $\log P$ | $\sigma$ | R- |
| 4.38 | 4.54 | 1.24 | 2.08 | 0.00 | H- |
| 4.65 | 5.00 | 0.00 | 2.58 | -0.17 | $\mathrm{CH}_{3}$ |
| 4.59 | 4.32 | $-0.07$ | 3.08 | -0.15 | $\mathrm{C}_{2} \mathrm{H}_{5}$ |
| 4.19 | 3.82 | $-0.36$ | 3.58 | -0.13 | $n-\mathrm{C}_{3} \mathrm{H}_{7}$ |
| 3.45 | 3.85 | $-0.39$ | 4.08 | -0.16 | $n-\mathrm{C}_{4} \mathrm{H}_{9}-$ |
| 2.84 | 2.74 | $-0.35$ | 4.38 | -0.23 | iso- $\mathrm{C}_{5} \mathrm{H}_{11}-$ |
| 3.71 | 3.40 | $-0.19$ | 1.55 | 0.06 | $-\mathrm{CH}_{2} \mathrm{OCH}_{3}$ |
| 3.68 | 3.82 | -0.47 | 1.53 | 0.52 | $-\mathrm{COCH}_{3}$ |
| 2.10 | 3.32 ${ }^{\text {a }}$ | $-0.39$ | 2.42 | -0.13 | $-\mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{OH}$ |
| 2.18 | $3.96{ }^{3}$ | $-0.36$ | 1.92 | -0.07 | $-\mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{OH}$ |
| 2.59 | $4.47^{\text {a }}$ | -0.07 | 1.42 | 0.06 | -- $\mathrm{CH}_{2} \mathrm{OH}$ |

${ }^{\text {a }}$ Calculated from Eq. $1 a$ of Table II. $b$ From Fig. 2 of Reference 4. c From Reference 19, $d$ Calculated from Eq. $2 c$ of Table II. e From Reference 9. $f$ From References 14 and 15.9 From Reference $13 .{ }^{i}$ Calculated from Eq. $3 a$ of Table II. ${ }^{i}$ From Reference 10. $i$ Calculated from Eq. 3 c of Table II. $k$ Estimated values. $l$ These points are not included in Eq. $3 b$ of Table II. $m$ Not measured. $n$ Calculated from Eq. $4 b$ of Table II. o From Reference II. $p$ These points are not included in Eq, $4 b$ of Table II. $q$ From Reference 12. r Calculated from Eq. 5 g of Table II. : These points are not included in Eq. $5 g$ of Table II.

Table II-Equations Correlating Enzyme Inhibition with Physicochemical Constants

| Enzyme | Inhibitors | Equation | $n$ | $r$ | $s$ | Eq. No. | $\begin{gathered} \log P_{0,} \\ (95 \% \mathrm{c}-\mathrm{I} .) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Lipoxygenase | ROH | $p K_{I}=0.954 \log P+0.329$ | 12 | 0.992 | 0.110 | $1 a$ |  |
|  |  | $p K_{I}=0.944 \log P+0.830$ | 12 | 0.984 |  | $1 b^{a}$ |  |
| Carbonic anhydrase | Sulfonamides | $p K_{I}=0.553 \log P+5.378$ | 19 | 0.609 | 0.492 | $2 a$ |  |
|  |  | $p K_{I}=1.026 \sigma+5.438$ | 19 | 0.886 | 0.288 | $2 b$ |  |
|  |  | $\begin{gathered} p K_{I}=0.259 \log P+0.886 \sigma+ \\ 5.314 \end{gathered}$ | 19 | 0.923 | 0.247 | $2 c$ |  |
| D-Amino acid oxidase | Maleimides (at pH 7.0 ) | $\log _{1.745} k^{\prime}=0.339 \pi+4.705 \sigma+$ | 8 | 0.988 | 0.085 | $3 a$ |  |
|  |  | $\log k^{\prime}=0.395 \pi+1.051$ | 6 | 0.999 | 0.018 | $3 b$ |  |
|  |  | $\log k^{\prime}=0.382 \pi+1.503$ | 6 | 0.999 | 0.019 | 3 c |  |
| Hydroxyindole-$o$-methyltransferase | $N$-Acyltryptamines | $\log 1 / I_{50}=0.561 \log P+1.590$ | 24 | 0.870 | 0.255 | $4 a$ |  |
|  |  | $\log 1 / I_{50}=0.601 \log P+1.491$ | 21 | 0.948 | 0.170 | $4 b$ |  |
| Monoamine oxidase | $\beta$-Carbolines | $\log 1 / I_{50}=0.675 E_{s}+4.017$ | 11 | 0.509 | 0.578 | $5 a$ |  |
|  |  | $\log 1 / I_{50}=-0.216 \log P+4.494$ | 11 | 0.355 | 0.628 | $5 b$ |  |
|  |  | $\begin{aligned} & \log 1 / I_{50}=-0.373(\log P)^{2}+ \\ & 1.907 \log P+1.864 \end{aligned}$ | 11 | 0.604 | 0.568 | 5 c | $\stackrel{2.56}{(\infty)}$ |
|  |  | $\begin{aligned} & \log 1 / I_{50}=0.454 E_{3}-0.304 \\ & (\log P)^{2}+1.564 \log P \\ & \quad+2.283 \end{aligned}$ | 11 | 0.648 | 0.556 | $5 d$ | $\stackrel{2.57}{(\infty)}$ |
|  |  | $\begin{aligned} & \log 1 / I_{50}=0.635 E_{s}+3.983 \\ & \log 1 / I_{50}=-0.215 \log P+4.550 \\ & \log 1 / I_{50}=-0.679(\log P)^{2}+ \end{aligned}$ | 8 | $\begin{aligned} & 0.507 \\ & 0.341 \end{aligned}$ | $\begin{aligned} & 0.649 \\ & 0.707 \end{aligned}$ | $\begin{aligned} & 5 e \\ & 5 f \end{aligned}$ |  |
|  |  | $3.719 \log P-0.422$ | 8 | 0.900 | 0.360 | $5 g$ | $\begin{aligned} & 2.74 \\ & (2.32-2.98) \end{aligned}$ |
|  |  | $\begin{aligned} & \log 1 / I_{50}=0.140 E_{s}-0.645 \\ & \quad(\log P)^{2}+3.544 \log P \\ & -0.227 \end{aligned}$ | 8 | 0.905 | 0.390 | 5h | $\begin{aligned} & 2.75 \\ & (1.99-3.13) \end{aligned}$ |

[^0]correlation is obtained ( $r=0.948$ for Eq. $4 b$ ). The authors also explored the role of the electronic parameter. For the 15 molecules with X - Ar as $\mathrm{R}_{2}$ (Table I), neither the $\sigma$ of X nor the $\sigma$ of $\mathrm{R}_{1}$ gives significant improvement in correlation. Of the three poorly predicted molecules, two may be due to steric hindrance, one with the methyl group as $\mathbf{R}_{3}$, and the other with the $3,4,5$-trimethoxybenzyl group as $R_{2}$. The fact that the observed activities of these three compounds are lower than the predicted values supports this argument. The third molecule has the 3,5 -dichlorophenyl group as $\mathrm{R}_{2}$. It is difficult to explain why this is poorly predicted since the one with the 3,4dichlorophenyl group as $\mathbf{R}_{2}$ is slightly more active than predicted.
For the inhibition of monoamine oxidase by 9 -substituted $\beta$ carbolines, Taft's steric constant, $E_{s}$, gives somewhat better correlation than $\log P$ (Eq. $5 a$ versus $5 b$ ). However, the correlation coefficients are too low to be considered significant. Even when a $(\log P)^{2}$ term is included, the correlation coefficient is still below 0.70 (Eqs. $5 c$ and $5 d$ ). When three compounds with an alcoholic OH group are excluded, a parabolic equation of $\log P$ gives fairly good correlation (Eq. $5 g$ ). The $(\log P)^{2}$ term in Eq. $5 g$ is significant at the 99 -percentile level ( $F_{1,5}=18.2 ; F_{1,5} 0.99=16.3$ ). For the eight compounds without an OH group, neither the linear equation of $E_{s}$ nor that of $\log P$ gives a good correlation (Eqs. $5 e$ and $5 f$ ); the addition of the $E_{s}$ term to the parabolic equation does not improve the correlation significantly (Eq. $5 h$ versus $5 g, F_{1,4}=0.21$ ). It is felt that an active function like an OH group may have its own intrinsic activity not possessed by the other inert substituents. For example, the $\mathbf{H}$ of the OH group might form a hydrogen bond with an atom having unshared election pair(s). The fact that the activities of the compounds with the OH group are appreciably higher than what are predicted from $\mathrm{Eq} .5 g$ is in accordance with this explanation. The optimum lipohydrophilic character $\left(\log P_{0}\right)$ for the maximum inhibition is derived by setting $\left(d \log 1 / I_{50}\right) /(d \log P)=0(17-19)$. This is the apex of the parabolic curve. Once this $\log P_{0}$ is obtained, it may serve as a useful guidepost in designing new inhibitors.

The importance of the hydrophobic interactions for the enzyme inhibition is clearly shown by the good correlations obtained by using $\log P$ or $\pi$ with or without a $\sigma$ term.

## DISCUSSION

From the correlations obtained, it is clear that in the five enzyme systems examined the lipohydrophilic character of the inhibitors plays a very important role in inhibition. The rather nonspecific hydrophobic interactions may be involved in two different ways: (a) adsorption and desorption on the macromolecule, since all proteins including enzymes contain $20-45 \%$ of amino acids with nonpolar side chains (20), and (b) inducing proper fit at the active site or the allosteric site (21) by the association of the nonpolar groups in the presence of water molecules. At present, not enough data are available to differentiate which of these two is more important.

It will be interesting to apply the method used in this study to other systems where drugs exert their activity by enzyme inhibition, such as choline esterase inhibitors and histidine decarboxylase inhibitors.

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[^0]:    ${ }^{a}$ From Reference 4.

